

## Data structures and algorithms

- 1) Consider a vector  $V[1..N]$  which contains  $N$  positive integer entries.
- a. [25 points] Use pseudo-code to describe an algorithm  $j=\text{FindLargest}(V)$  which returns  $L$  as the *index* of the largest entry of vector  $V$  (without modifying its contents) with complexity  $O(N)$ .
  - b. [25 points] Use pseudo-code to describe an algorithm  $S=\text{Sort}(V)$  which returns a sorted vector  $S[1..N]$  and uses  $\text{FindLargest}(V)$  as a function to assist in the sorting of the entries in  $V$ . You can use temporary variables and vectors. What is the complexity of your sort algorithm?
  - c. [50 points] The use of heap data structures can lead to faster sorting. Consider a heap data structure implemented as a binary tree.
    - i. What is the property that must be satisfied for every node “ $i$ ” (except the root node) of the binary tree for it to be a heap?
    - ii. Consider the implementation of  $\text{FindLargest}$  using a heap:  
 $p=\text{FindLargest}(H)$  returns a *pointer* to the heap node which stores the largest element of the heap (without modifying its contents). Can this algorithm achieve lower complexity than the algorithm in part a)?
    - iii. Describe how the  $\text{Sort}()$  algorithm would need to be modified to work with a heap data structure and the  $p=\text{FindLargest}(H)$  function. What is the complexity of the modified  $\text{Sort}()$  algorithm?

# Operating Systems

2) This question considers a typical UNIX-like multi-user, multi-task operating systems which employs virtual memory, processes, and preemptive CPU schedulers to support time-sharing of resources among multiple tasks. In answering the five parts of this question, state your assumptions if necessary.

i) [20 points] Describe two major constituents of the context of a running process.

ii) [20 points] Consider a process “fork” event. Describe when and how the different constituents of the context of the parent process are copied to the child process.

iii) [20 points] Describe one hardware event and one software event that can trigger the execution of the O/S kernel scheduler and a context switch.

iv) [20 points] Why does an O/S kernel flush the contents of the translation look-aside buffer when a process context switch is performed?

v) [20 points] Why is it typically faster for the O/S kernel to switch among threads of a process than it is to switch process contexts?